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### collapse: a clinical study of a financial crisis East Asia and Europe during the 1997 Asian

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### Abstract

played a major role. © 2002 Elsevier Science B.V. All rights reserved course, that it was the cause rather than the effect of the crisis. Exchange rate volatility in Asia is reason enough for large declines in asset values though one cannot prove, of crisis; this was reversed during the crisis. The observed decline in diversification potency larger in Asia. Diversification potential was better in Asia than in Europe before the with the onset of the crisis. Covariances, correlations, and volatilities increased from the volatility contagion in the pre-crisis era but that susceptibility increased significantly around the crisis, fomenting investor fears of contagion and reducing asset values pre-crisis to the crisis period in both regions, but the percentage increases were much this inquiry. We find that European and East Asian countries were not susceptible to because of lower diversification potential. Statistical measures are developed to aid 1997 Asian crisis. The clinical issue is whether regional inter-dependence became larger Asian stock markets are compared with European markets before and during the

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investor affected by changes, if any, in the regional structure of return comore closely connected than other neighboring countries? Was the rapid about linkages among stock markets in general. How closely are stock simultaneous misfortune of so many countries has raised questions movement? linkages evolved over time? Finally, how was the international portfolio the contrary, did the crisis mark a break from the past? How have interspread of the crisis in Asia predictable from strong prior inter-relations or, to markets in neighboring countries related? Are East Asian stock markets of its local stock value, Hong Kong 32%, Indonesia 34%, Malaysia stock market indices plunged in most countries. Thailand lost about 33% 42%, Philippines 32%, Singapore 10%, and South Korea 44%. The nearly dollar terms, Hong Kong 33%, Indonesia 71%, Malaysia 57%, Philippines six months that followed, Thailand lost 65% of its stock market value in On July 2, 1997 the Thai baht broke its peg to the US dollar. In the Singapore 24%, and South Korea 72%. Both currencies and local

countries during the mid-90s and by contrasting it to that among West analyzing the regional interdependence among stock markets of East Asian paper also tries to answer the questions raised in the previous paragraph by stock markets. In doing so, it constructs some new statistical measures. The develops a method for studying co-movements among a group of national the overall structure of relations within a group of countries. This paper often, but past literature provides scant guidance about how to measure of countries. Relations between pairs of countries have been studied co-movements of national stock returns within a region or a group European countries. To answer these questions, we require a method for characterizing

of Asian markets before and after this landmark event. This subject, which ones, is where we aim to make a contribution. seems of critical importance in understanding the crisis and averting future to explain the phenomenon; yet little has been done to compare co-movements The crisis justifiably engendered theoretical and empirical research attempting term co-movement and its stability had not been subjected to extensive inquiry. linkages among Asian stock markets (e.g., Chung and Liu, 1994) but short-Prior to the crisis, there had been some empirical literature on the long-term

useful in answering them. Section 5 presents the empirical evidence. Section 6 Section 4, we state the basic research questions and design some statistical tools concludes and offers suggestions for future research East Asian financial markets. Section 3 describes the data to be examined. In important research findings in the areas of stock market inter-linkages and The paper is organized as follows. The next section summarizes the

participants in the Georgia Tech/Fortis international finance conference and the 2000 European Edwards, Yasushi Hamao, Andrey Pavlov, Avanidhar Subrahmanyam, John Wald and Financial Management Meetings in Athens. <sup>27</sup>The authors gratefully acknowledge constructive comments and suggestions from Sebastian

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### 2. Previous literature

Using the then newly developed method of co-integration, Kasa (1992) studied the long-term equilibrium relations among five developed capital markets and extracted a common trend that strikingly captured their movements. Subsequent contributions included Arshanapalli and Doukas (1993) and Chung and Liu (1994). Richards (1995), however, questioned Kasa's conclusions and argued that while national stock markets exhibit predictability, there is little evidence of co-integration.

Another branch of the literature has examined the evolution of correlation among a group of countries over time. Important contributions here include Kaplanis (1988), Koch and Koch (1991) and Longin and Solnik (1995). Kaplanis (1988) traced the stability of the co-movements among monthly stock index returns for ten industrial countries between 1967 and 1982; she found stability in correlations but not in covariances. Koch and Koch (1991) studied co-movements of daily returns in six industrialized and two developing countries between 1972 and 1987; they found strong interactions among markets on the same day and they also documented changes over time in the correlation structure. Among developed countries between 1960 and 1990, Longin and Solnik (1995) concluded that both covariances and correlations were unstable.

In related work, Dumas et al. (2000) study whether observed stock market correlations are consistent with cross-country correlations in national output. They find that equity correlations are indeed better in accord with global integration than with segregation. Since the structural correlations among national outputs could vary over time, their work implies that equity correlations also could be time varying. This is directly tested by Bansal and Lundblad (2001), who find time variations in cash flow growth rates and risk premiums that are consistent with movements in conditional correlations among country equity returns.

Hamao et al. (1990), King and Wadhwani (1990) and others have investigated "spillovers" in volatility and expected returns from one country to another. The former used a GARCH model to measure spillover while the latter used contemporaneous correlations. Volatility spillover is an important concept because it attempts to identify directional causality between disturbances in two countries. An extension and variation of this approach will be adopted hereafter.

Some studies have looked at East Asian countries in particular. Chung and Liu (1994) found that the US and five East Asian countries have co-integrated stock prices. So et al. (1997) examined the volatility of and correlations among seven Southeast Asian stock markets between 1980 and 1991 and attempted to group countries into interconnected blocks.

The Asian crisis itself has elicited quite a few papers. The role of currency has received much attention, (see Kamin, 1999; Fernald et al., 1999; Masson, 1999). Banks and regulators have received their share of criticism, (see Kane, 2000) but Kho and Stulz (2000) find little evidence that banks as a group or the International Monetary Fund were prime culprits. Few papers have viewed the crisis from the perspective of an international portfolio investor, yet many, notably including the Malaysian prime minister (Mohamad, 1997), have blamed international fund managers for the crisis. Brown et al. (2000) counter this view in the case of hedge funds.

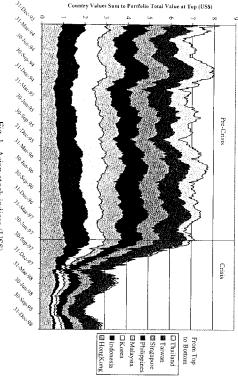
There have also been several recent papers—both theoretical and empirical—focused on financial contagion. Baig and Goldfajn (1998) posit that a rise in correlation levels as compared to "tranquil" periods is an indication of contagion and find such an effect during the Asian Crisis. Boyer et al. (1997) and Forbes and Rigobon (1999) argue that such a finding may be the artifact of the statistical method. Bae et al. (2000), adopting a technique from health sciences, use a multinomial logistic regression to compare the levels of contagion of extreme return shocks across countries in two regions—Latin America and Asia.

In a recent assessment of the literature, Chowdhry and Goyal (2000, p. 135) conclude that most theoretical explanations of the Asian crisis are "disappointing" in their "out-of-sample performance". They call for an alternative diagnosis. Our clinical study responds by comparing the afflicted patient, East Asia, with a healthy Europe. We compare the relative strength of market linkages within each region and attempt to determine whether Asia's linkages underwent a fundamental change during the crisis. While we look at relationship between returns in two regions before and during the Asian crisis like Bae et al. (2000), our focus is on studying the changes in the degree of comovement in Asian returns during the crisis, rather than the contagion in extreme movements, the central focus of Bae et al. (2000).

The available data are daily close-to-close returns for indices of eight East Asian countries that experienced a crisis of some severity in 1997. Data were also collected for a matching sample of eight West European non-crisis countries. The Asian countries are Hong Kong, Indonesia, Malaysia, the Philippines, Singapore, South Korea, Taiwan and Thailand while the European countries are France, Germany, Italy, the Netherlands, Portugal, Spain, Switzerland, and the United Kingdom. The two groups are of equal size for ease of comparison and the European matching sample consists simply of the largest countries augmented with two arbitrarily chosen smaller countries for a total of eight.

Buy-and-Hold Portfolio with \$8 Initial Value;\$1/Country on December 31, 1993

6



Time zone differences within either region do not exceed two hours: Fig. 1. Asian stock indices (US\$)

Descriptive statistics, country returns by sub-period

Daily country index returns (%/day) are denominated in US dollars and tabulated for the pre-crisis period, December 31, 1993 through July 1, 1997,

	Hong Kong	Indonesia	Korea	Malaysia	Philippines	Singapore	Taiwan	Thailand
				Pre-ci	risis			
Mean	0.0240%	0.0189%	-0.0291%	-0.0149%	-0.0006%	-0.0152%	0.0375%	-0.1133%
Standard deviation	1.3003%	1.0190%	1.2513%	1.3010%	1.1475%	0.8777%	1.5531%	1.6187%
Kurtosis	3.882	3.919	1.282	8.243	2.334	4.951	3.471	2.659
Skewness	-0.514	-0.144	-0.022	0.103	-0.242	-0.233	-0.168	-0.085
Minimum	-7.72%	-5.28%	6.03%	-7.48%	-6.20%	5.24%	-7.39%	-7.80%
Maximum	5.63%	6.47%	6.04%	9.97%	4.80%	5.52%	6.62%	6.45%
				Cris	is			
Mean	-0.1319%	-0.4242%	-0.1118%	-0.2756%	-0.1981%	-0.1095%	-0.1244%	0.1994%
Standard deviation	2.7300%	6.4720%	4.4184%	4.0963%	2.8091%	2.2490%	1.9586%	3.5978%
Kurtosis	5.908	7.942	3.938	6.655	1.650	3.234	2.078	2.379
Skewness	0.437	-0.947	0.044	0.611	0.117	0.348	-0.131	0.764
Minimum	-13.63%	42.84%	19.18%	-22.04%	-10.24%	-9.59%	-8.98%	-9.38%
Maximum	15.37%	21.48%	20.12%	22.20%	11.56%	9.94%	6.72%	17.44%
	France	Germany	Italy	Netherlands	Portugal	Spain	Switzerland	UK
				Pre-ci	risis			
Mean	0.0252%	0.0432%	0.0357%	0.0730%	0.0586%	0.0647%	0.0643%	0.0421%
Standard deviation	0.8509%	0.8357%	1.3396%	0.7257%	0.7833%	0.9208%	0.8361%	0.6511%
Kurtosis	1.150	1.046	1.431	1.761	4.213	1.716	1.488	0.756
Skewness	-0.135	0.341	0.028	-0.343	-0.175	- 0.399	-0.080	-0.256
Minimum	-3.71%	-3.71%	-5.68%	-4.02%	-5.20%	-5.36%	-3.31%	-2.97%
Maximum	3.09%	2.64%	6.02%	2.43%	3.75%	3.12%	3.55%	2.26%
				Cris	sis			
Mean	0.0936%	0.0636%	0.1544%	0.0639%	0.0903%	0.0999%	0.0767%	0.0532%
Standard deviation	1.2811%	1.4600%	1.7452%	1.4338%	1.4828%	1.5641%	1.3189%	1.0438%
Kurtosis	1.923	1.239	1.176	1.090	2.912	2.396	1.810	1.028
Skewness	-0.030	-0.371	-0.211	0.061	-0.417	-0.255	0.082	-0.034
Minimum	-4.74%	5.55%	6.40%	4.89%	-6.72%	-6.02%	-4.09%	-3.14%

groups of countries over the entire sample and for the pre-crisis and crisis

Internet address http://www.stern.nyu.edu/~nroubini/asia/AsiaHomepage.html

Table I provides descriptive statistics of the dollar-valued returns for both

crisis periods by plotting an initially equal-weighted portfolio of the eight 913 points before. Fig. 1 provides an overall depiction of the pre-crisis and Our data sample thus includes 392 observations during the crisis period and generally identified as the first time that a real crisis was apparent; (see, for

Asian countries

devaluation, that of the Thai baht. There had been previous storm warnings,

the beginning of the Asian crisis. On this date occurred the first major

12/31/98, 1305 daily returns. We rather arbitrarily selected July 2, 1997 to be dollar value of the index at time t. The data cover five years from 12/31/93 to returns are computed by using the formula  $ln(P_t/P_{t-1})$  where  $P_t$  refers to the using the daily closing exchange rate obtained from the same source. Dollar

particularly a "speculative attack" on the baht in mid-May, but July 2 has been

instance, the chronology of the Asian crisis constructed by Nouriel Roubini1)

co-movements. Daily closing stock index levels in local currency are from

hence, contemporaneous daily data can be employed in computing DATASTREAM. The local currency stock index value is converted to dollars

sub-samples. While the Asian countries all experienced negative average returns during the crisis period, no European country shared that experience; indeed, returns were higher than in the pre-crisis period for every European country. Fig. 2a, plots the mean returns to emphasize just how different the crisis period was in the two regions. The volatility of returns went up in the crisis period for every single country in both regions. In Asia, volatility was roughly three times higher (on average) during the crisis period; in Europe, it was about 1.5 times higher (Fig. 2b).

### l. Research questions and statistical tools

Our research agenda can be captured in a few questions: How susceptible are countries to volatility spillover and how did this susceptibility change during the Asian crisis? What proportion of intertemporal changes in covariances among countries is attributable to changes in correlation and what proportion to changes in variance? How has the ability to diversify within a region evolved over time? Each of these questions is critically important to the international investor. Volatility spillover, or contagion, implies that countries will become more or less risky around the same time. Evolution of the covariance structure alters the available degree of diversification and thus changes the risk/return tradeoff for portfolio investors. The mere possibility of either phenomenon has the potential to induce investor panic and throughout a region.

First, we look at volatility "spillover" from one market to another and seek to determine whether spillover intensity changed during the 1997 crisis. An increase in spillover intensity would be evidence of greater contagion around the crisis. This issue was investigated by King and Wadhwani (1990), among others, during the pandemic October 1987 crash. We change their now standard approach slightly so as to measure the overall susceptibility of countries within a region to volatility shocks imported from neighbors.

To measure volatility spillover, we regress weekly first differences of daily volatility (from dollar-denominated returns of a country's stock index) on lagged values from other countries in the region. Specifically, the regression model is

$$\Delta \sigma_{i,\,t} = \alpha_i + \Sigma_j [\beta_{i,\,j} \Delta \sigma_{j,\,t-1} + \Delta \beta_{i,\,j} \delta_t \Delta \sigma_{j,\,t-1}] + \varepsilon_{i,\,t}, \tag{1}$$

where  $\sigma_{i,t}$  is the estimated volatility computed from daily dollar-valued returns during week t in country i,  $\Delta \sigma_{i,t} = (\sigma_{i,t} - \sigma_{i,t-1})$  is the weekly first difference, and  $\delta_t$  is an indicator variable which is zero in the pre-crisis period and unity during the crisis period. The average values of the weekly volatilities of the

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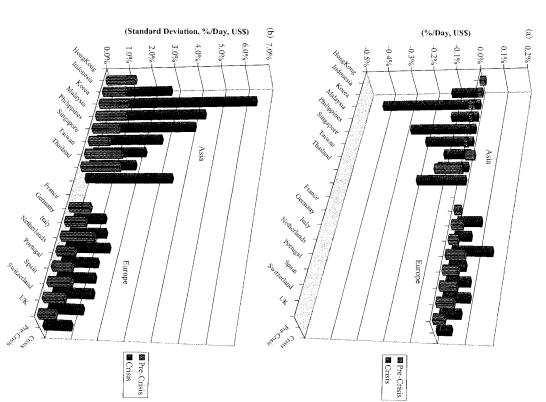


Fig. 2. (a) Mean returns by region and period. (b) Volatility by region and period

The table reports time series mean values of  $c_{t,i}$ , the estimated standard deviation of daily dollar-denominated returns during week t in country i.

	Pre-crisis (181 weeks)	Crisis (77 weeks)
Asia		
Hong Kong	0.97%	2.04%
Indonesia	0.73%	4.45%
Korea	1.00%	3.08%
Malaysia	0.93%	2.83%
Philippines	0.86%	2.10%
Singapore	0.67%	1.64%
Taiwan	1.19%	1.51%
Thailand	1.22%	2.65%
Europe		
France	0.69%	1.03%
Germany	0.68%	1.21%
Italy	1.06%	1.40%
Netherlands	0.59%	1.16%
Portugal	0.60%	1.11%
Spain	0.74%	1.22%
Switzerland	0.66%	1.03%
UK	0.53%	0.84%

daily returns, the  $\sigma_{i,i}$ 's, for the different countries in the two regions in the precrisis and the crisis periods, are presented in Table 2.

First, we test whether there is evidence of volatility spillover of the same magnitude spanning the pre-crisis and crisis periods. The test's null hypothesis is that the  $\beta_{i,j}$  (as opposed to the slope changes,  $\Delta \beta_{i,j}$ ), are all zero. For each region, we estimate all eight regressions (1) as a system and construct a joint test, i.e.,

$$\mathbf{H}_0: \beta_{i,j} = 0 \quad (j \neq i, \quad \forall i, j).$$
 (2)

This involves a simultaneous test that 56 coefficients, seven slope coefficients in eight regional equations, are significantly different from zero.<sup>2</sup> Note that this test involves only the *inter*-country coefficients and therefore assesses spillover. Volatility dependence across time *within* a country does not involve spillover and should be assessed separately (see below).

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The "slope dummy"  $(\delta_l)$  in (1) allows us to test whether the 1997 Asian crisis was marked by a change in volatility spillover. The null hypothesis is

$$\mathbf{H}_0: \Delta \beta_{i,j} = 0 \ (j \neq i, \quad \forall i, j). \tag{3}$$

The test does not restrict the change in spillover susceptibility, if any, to be of a particular sign, though one might intuitively anticipate an increase in susceptibility during a crisis.

To be complete, we also record the evidence on volatility serial dependence within countries during both periods ( $\mathbf{H}_0: \beta_{i,j} = 0 \quad \forall i$ ) and test whether there has been a change in such dependence from the pre-crisis to the crisis period ( $\mathbf{H}_0: \Delta\beta_{i,j} = 0 \quad \forall i$ ).

Our second research question asks about return covariances among

Our second research question asks about return covariances among countries within a region and how those covariances changed near the crisis. The importance of the covariance to the international portfolio investor can hardly be over-emphasized; mean-variance efficient portfolios are determined in large part by the covariance matrix. Consequently, significant change in the regional covariance structure can explain why investors might reduce their holdings; the benefits of diversification across those markets have become less compelling.

We also hope to uncover the sources of changes in covariance. Independent but contemporaneous disturbances in different countries will affect covariance but not correlation. Sympathetic movements among stock markets will raise the correlation as well. Understanding the covariance structure requires decomposition into correlation and variance; thus decomposition is proposed and implemented in this paper. The relative importance of one component over the other provides a better understanding of the nature of co-movements among the markets. We estimate whether correlation played the dominant role during the crisis and also whether the correlation/variance decomposition is significantly different in Asia and Europe.

There are no standard methods for testing the structural evolution of correlation or covariance matrices. Apart from long-horizon co-integration, the typical approaches have compared correlation matrices at two points in time (e.g. Longin and Solnik, 1995) or the evolution of pair-wise correlations. The first approach does measure a group effect but only at two points in time; it is not easily adapted for tracing the evolution in between. The latter approach can capture the evolution through time but does not measure any group effect. This situation would be improved if the information in a covariance or correlation matrix could be summarized in a single scalar. The evolution of such a scalar could be studied with univariate techniques. Moreover, movements in covariances could be more easily decomposed into its constituents, correlations and variances, which might provide insights into the fundamental determinants of structural change. We propose a battery of such scalar measures and apply them in studying the Asian crisis.

<sup>&</sup>lt;sup>2</sup>This test explicitly allows spillover to be either positive or negative. Although one might intuitively think of volatility increases spilling over as increases elsewhere, or vice versa, the opposite is conceivable.

pair of countries in a region; propose the geometric mean of absolute values of the covariance between every To summarize information in the covariance matrix in a single number, we

$$\gamma_{\text{cov}} = \left[ \prod_{i \neq j} |\text{cov}_{ij}| \right]^{1/[m(m-1)/2]}$$

where m is the number of countries. A corresponding measure for correlation is

$$\gamma_{\text{corr}} = \left[ \prod_{i < j} |\text{corr}_{ij}| \right]^{1/[m(m-1)]}$$

individual returns Finally, we compute the geometric mean of the standard deviations of the

$$\left(\gamma_{\sigma} = \left[\prod_{i=1}^{m} \sigma_{i}\right]^{-1}\right).$$

These measures not only capture the information in the covariance and correlation matrices but are also connected by the simple identity.<sup>3</sup>  $\gamma_{\rm cov} = \gamma_{\rm corr} \gamma_{\sigma}^2$ . Thus, the log first difference between two periods is

$$\Delta \log \gamma_{\rm cov} = \Delta \log \gamma_{\rm corr} + \Delta \log \gamma_{\sigma}^{2} \tag{4}$$

relative importance of correlation can be measured by Assuming that correlation and volatility change in the same direction, the percentage changes (continuously compounded) and are thus dimensionless. correlation components. Note that log first differences are equivalent to which provides a decomposition of covariance change into its volatility and

$$\eta = |\Delta \log \gamma_{\text{corr}}|/(|\Delta \log \gamma_{\text{corr}}| + |\Delta \log \gamma_{\sigma}^2|)$$
 (5)

variance were relatively more prominent causes of movements in covariance Evolution of the  $\eta$  statistic should reveal points in time when correlation and is the contribution of correlation (volatility) to the change in covariance which is bound between 0 and 1. The higher (lower) the value of  $\eta$ , the greater

individual countries per se. general trend of inter-linkages within each regional group rather than on attempts to capture an array of numbers. The justification is our focus on the involve some loss of information as any single number necessarily would if it covariances and correlations of stock returns in the two regions. This does Geometric means  $\gamma_{cov}$  and  $\gamma_{corr}$  are intended to compactly summarize

region is of fundamental importance given the crucial role of the correlation The evolution and stability of the correlation matrix of returns within a

correlation matrices developed in Jennrich (1970). For any two p-variate ion matrices, we adopt a test statistic for the equality of two or more sample correlation matrices  $R_1$  and  $R_2$  of sample size  $n_1$  and  $n_2$  respectively, the structure in portfolio formation. To measure the evolution of correlat-Jennrich  $\chi^2$  is given by

$$\chi^2 = \frac{1}{2} \text{tr}(Z^2) - dg'(Z) S^{-1} dg(Z), \tag{6}$$

equal,  $\chi^2$  is distributed asymptotically as  $\chi^2$  with p(p-1)/2 degrees of freedom. and diagonal of a matrix, respectively. If the true correlation matrices are crisis period.  $n_2$ ) and  $S = (\delta_{ij} + \bar{r}_{ij}r^{ij})$ . Here  $\delta_{ij}$  is the Kronecker delta,  $\bar{r}_{ij}$  is an element of where  $Z = c^{1/2} \bar{R}^{-1} (R_1 - R_2), \ \bar{R} = (n_1 R_1 + n_2 R_2)/(n_1 + n_2), \ c = n_1 n_2/(n_1 + n_2)$ periods, we can test whether they have changed; e.g., from the pre-crisis to the Consequently, by computing correlation matrices from two different time  $\vec{R}$  and  $\vec{r}^{ij}$  is an element of  $\vec{R}^{-1}$ . The expressions "tr" and "dg" refer to the trace

investor have fared by creating an efficient allocation within a region? Would traced over time and compared across periods and regions. direct empirical measure of diversification potential, a measure which can be frontier, the less effective diversification. Hence estimated curvature provides a frontier and in particular by its curvature. The more sharply curved the thereafter? These questions are answered by the shape of the regional efficient diversification be more potent in Asia or in Europe, before the crisis or potential directly. How well (in mean-variance terms) would an international changes in investment opportunities around the crisis: calculate diversification There is an alternative and perhaps more direct approach to measuring

frontier can be described by the equation The mathematics of the efficient frontier, (e.g., Roll, 1977) show that the

$$\sigma_p^2 = (a - 2br_p + cr_p^2)/(ac - b^2),\tag{7}$$

where  $\sigma_p^2$  is the variance of efficient portfolio p and  $r_p$  is its mean return. The efficient set constants are given by  $a = E'V^{-1}E, b = E'V^{-1}I$ , and  $c = \iota'V^{-1}I$ , matrix, and t is the unit vector. With a little rearrangement, (7) can be written as where E is the mean return vector of n assets, V is their variance–covariance

$$(\sigma_p^2 - 1/c) = [c/(ac - b^2)](r_p - b/c)^2$$
(8)

which is the equation for a parabola with curvature  $\hat{c}^2(\sigma_p^2)/\hat{c}(r_p)^2 \equiv C =$  $2c/(ac-b^2)$ . The average level of C and its evolution in the two geographic regions provide the direct measures we seek of diversification potential.

markets in East Asia and how they differed from those among European stock and characterizing regional interdependence of markets in general markets. We hope also that these constructs will refine methods for studying bring out a comprehensive picture of the short-term relations among stock Taken as a battery of statistics, the above empirical constructs should help

This can easily be verified by expanding the expression for  $\gamma_{corr}$  and reorganizing the terms

### . Empirical results

### 5.1. A graphical portrayal

To depict graphically the evolution of relations among stock markets, we make calculations within overlapping windows of pre-specified length. Each window excludes the first daily observation from the previous window and adds one more daily observation in sequence. Hence successive values of the statistics are analogous to moving averages.

For regional (geometric) averages of covariance, correlation, and volatility, ( $\gamma_{cov}$ ,  $\gamma_{cor}$  and  $\gamma_o^2$ ), a six-month window gives the values plotted in Figs. 3–5. The spike in  $\gamma_{cov}$  for the East Asian countries in Fig. 3 coincides with the Asian crisis and appears to represent a significant break from the past. Before the crisis, Asia had a slightly lower covariance than Europe on average, but this was reversed dramatically during the crisis. Around the middle of the crisis period,  $\gamma_{cov}$  fell substantially in Asia, though it remained at a level much higher than the pre-crisis period and considerably higher than in Europe.

The European countries too display an increase in covariance during the crisis period. The largest part of the rise in Europe came later and was less pronounced than in Asia. Unlike Asia, no mid-crisis period downturn is visible in Europe; there is a sharp second upward movement instead.

Did correlations within the two regions move as much or can some part of the spikes in covariance be explained by higher volatility? Figs. 4 and 5 present

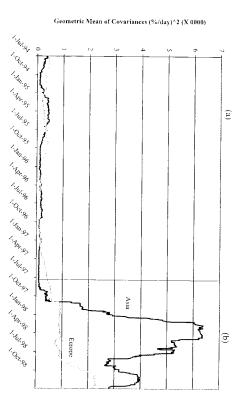


Fig. 3. Regional average covariance. (a) Pre-crisis; and (b) crisis

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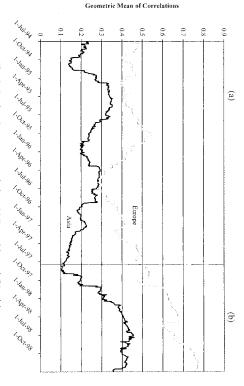


Fig. 4. Regional average correlation. (a) Pre-crisis; and (b) crisis

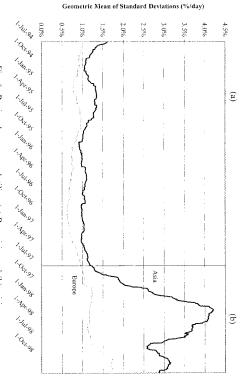


Fig. 5. Regional average volatility. (a) Pre-crisis; and (b) crisis.

visual evidence about this question. Fig. 4 shows an upward trend in correlation among European countries which appears to begin up to a year before the crisis and continues during the crisis period. This rise in correlations in Europe perhaps had more to do with the movement towards a monetary union than the Asian crisis. During the crisis, European and Asian countries displayed concurrent upward trends in correlation. Asia's trend was sharper near the beginning of the crisis but it leveled off and began to turn down in late 1998 while Europe's continued upward after a temporary dip in late April of 1998.

Fig. 5 plots average volatility. The similarity of the pattern to covariance (Fig. 3) is obvious even visually. Prior to the crisis, volatility was slightly higher in Asia than in Europe. The gap widened substantially as the crisis deepened and then narrowed toward the end of 1998.

The Jennrich  $\chi^2$  statistic, measuring the stability of the correlation matrix, is computed in a different fashion. Here one-year overlapping windows are each divided into two six-month sub-periods; the statistic compares correlation matrices between the sub-periods. Hence, each one-year window yields one value of the Jennrich  $\chi^2$ . Successive windows drop the first day from the previous window and add the day after the previous last day. Fig. 6 plots the p-value from the Jennrich test of the hypothesis that the two adjacent sixmonth periods have the same correlation matrix, so values near zero imply a strong likelihood that the matrix has changed.

For both Europe and Asia during the pre-crisis period, there are many large p-values; i.e., little evidence of an evolving correlation matrix. There are some near zero but then this statistic like any other has unavoidable sampling variation. The striking feature of Fig. 6 is that Asia's p-value falls essentially to zero during the crisis and remains there throughout. The Jennrich  $\chi^2$  p-value is also relatively low for Europe during the crisis period, but not persistently as low as for Asia.

Fig. 7 depicts the evolution of the sample curvatures of efficient frontiers within the Europe and Asia regions before and during the 1997 crisis. Each point gives the curvature of a sample efficient frontier constructed from daily return data for six months ending on the plotted date. Higher curvature implies less effective diversification within the region.

For about 18 months prior to the crisis and for six months into the crisis, Asia's curvature was lower than Europe's. This no doubt reflects similarities

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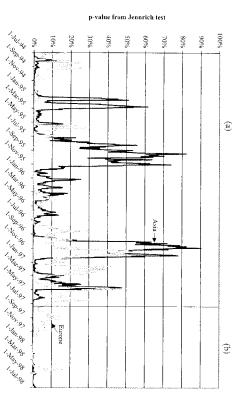


Fig. 6. Jennrich test of equality in successive correlation matrices. (a) Pre-crisis; and (b) crisis

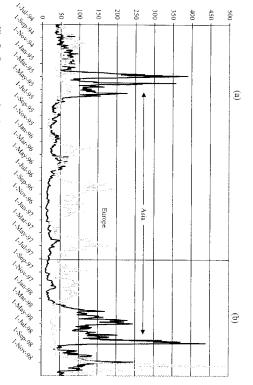


Fig. 7. Curvature of regional sample efficient frontiers. (a) Pre-crisis; and (b) crisis.

<sup>&</sup>lt;sup>4</sup>Because of the rolling window, there is considerable dependence across time in these plotted numbers. For instance, the dip in European correlation in the last few days of April 1998 was probably induced by dropping a few observations from the window. These same observations induced the sharp rise in the computed average correlation around late October 1997, six months earlier.

<sup>&</sup>lt;sup>5</sup>The plot stops in mid-1998 because the Jennrich statistic requires a six-month sample before and after the plotted date.

<del>-</del>2

among European economies and the concomitant smaller potential for diversification. By early 1998, however, Asia's curvature had increased dramatically and exceeded Europe's by a sizeable margin. By this time at least six months of the crisis period fell within the window's calculation. Perhaps surprising, late 1998 saw a sharp reduction in Asia's curvature followed by an even sharper increase in curvature for Europe. This is consistent, of course, with the relative movements of the average covariances in the two regions (Fig. 3) around the same time.

### 5.2. Statistical tests

The pictures discussed above seem to portray remarkable changes within Asia during the 1997 crisis and less dramatic but still noticeable changes in Europe. But in dealing with statistics, a picture's value may not rise to its purported worth of a thousand words. Indeed, intra-ocular tests based on pictures are often misleading. To be assured of reliable inferences, one is obliged to adopt more formal methods.

### 5.2.1. Volatility spillover

Table 3 reports tests for the presence of volatility spillover effects before and during the crisis in both regions. The first hypothesis, (2), that volatility spillover was present in pre-crisis and crisis periods and had the same intensity in both, is not supported by the evidence in either region. Neither *p*-value in the first row of Table 3 is even close to significant.

In contrast, there is strong evidence of spillover in Asia during the crisis, a *p*-value of 0.000 rejecting hypothesis (3). There is also evidence, (*p*-value 0.00221) that volatility spillover increased in Europe.

Given previous literature, it is not surprising that volatility changes are highly serially dependent within countries after accounting for spillover; this is documented by the p-values in the third row of Table 3; they are zero to three decimal places in both regions. Interestingly, the "own" coefficients  $\beta_{i,i}$  from model (1) (not reported) are mostly negative. There is no evidence of a change within Asia of this intra-country dependence from pre-crisis to crisis, (the p-value is 0.222 for a test that  $\Delta\beta_{i,i} = 0$  jointly for all i). There is some evidence, however, that Europe experienced a change (p-value 0.0310). It would seem that Europe became more generally serially dependent after the beginning of the Asian crisis both within each country and across countries. Asia differed from Europe because there was no significant increase in volatility serial dependence intra-country.

Whatever the underlying causes of Asia's crisis might have been, they apparently induced a structural change in the propensity of Asian countries to import recent volatility disturbances from their neighbors. Remember that (1) measures very short-term contagion, volatility that appeared in neighboring

### Tests for volatility spillover and for serial dependence

For each of two regions, Asia and Europe, a system of eight simultaneous equations is estimated using USS-denominated country index daily returns. There is one equation per country in the form  $\Delta \sigma_{l,l} = \alpha_l + \sum_l \beta_{l,l} \Delta \sigma_{j,l-1} + \Delta \beta_{l,l} \bar{\beta}_l \Delta \sigma_{j,l-1}] + \epsilon_{l,l}$  where  $\sigma_{l,l}$  is the estimated volatility computed from daily returns during week l in country l,  $\Delta \sigma_{l,l} = (\sigma_{l,l} - \sigma_{l,l-1})$  is the weekly first difference,  $\delta_l$  is an indicator variable which is zero in the pre-crisis period and unity during the crisis period, and  $\epsilon_{l,l}$  is a disturbance not necessarily independent across equations (countries). Joint tests that the  $\beta_{l,l}$ 's for  $j \neq l$  are all zero would be rejected if there is evidence of volatility spillover in both the pre-crisis and crisis periods of the same intensity. Joint tests that the  $\Delta \beta_{l,l}$ 's for  $j \neq l$  are all zero would be rejected if volatility spillover changed (and was statistically more significant) during the crisis period. Joint tests that the  $\beta_{l,l}$ 's are all zero would be rejected if there was a change in within-country volatility dependence from the pre-crisis to the crisis period. The sixteen countries are listed in Table 1. There are 258 weekly observations. To save space, the estimated coefficients and other statistics are not reported but will be provided to interested readers upon request.

0.000	0.222	$\Delta \beta_{i,i} = 0, \forall i$
	0.000	$\beta_{i,i} = 0, \forall i$
		Serial dependence within countries
0.00221	0.000	$\Delta \beta_{i,j} = 0, (j \neq i, \forall_{i,j})$
0.548	0.999	$\beta_{i,j} = 0, (j \neq i, \forall_{i,j})$
		Spillover across countries
p-value		Null hypothesis
Europe	Asia	

countries just a few days earlier (i.e., in the previous week). In the pre-crisis period, there was no evidence at all of such contagion. It would be interesting to know whether such a marked increase in contagion is a general feature of crises.

# 5.2.2. Variability, co-movement, and efficient frontier curvature

Regional geometric averages of covariances, correlations, volatilities, and efficient frontier curvature are non-linear and would have complicated sampling distributions even if returns were Gaussian. This is all the more problematic because kurtosis statistics (Table 1) show the departure from Gaussian typical of asset returns. Hence, tests of statistical significance would be very difficult to develop analytically. It seems doubtful that GMM or similar methods can be exploited to obtain standard errors for our non-linear constructs, particularly in light of the large cross-section and relatively limited time period of the sample. Hence, the simplest approach appears to be resampling from the original data; i.e., employing the "bootstrap".

<sup>&</sup>lt;sup>6</sup>A basic reference on the bootstrap is Efron (1982).

Our resampling plan adheres faithfully in every instance to the procedures actually used in computing the sample point estimate from the data. To give a concrete example, suppose we wish to test whether covariances within a region, say Asia, increased from the pre-crisis to the crisis period. The point estimate would simply be the difference between the geometric averages for the Asian region in the two periods; i.e., \( \gamma\_{\text{cov},Asia,Crisis} - \gamma\_{\text{cov},Asia,Pre-Crisis} \). The first of these averages is calculated from 913 observations while the second is based on 392 observations, those being the numbers of daily returns available in the two subperiods.

Resampling for this statistic thus involves first selecting 913 calendar dates at random (with replacement) along with the actual daily returns for the eight Asian countries on those dates. Next, a second random selection of 392 calendar dates and their corresponding returns are selected. Covariances among the eight countries are computed for the two samples separately. Their geometric averages are then differenced to produce Ycov, Asia, Sample#1. The random selections are repeated 10,000 times, thereby generating a sampling distribution for 10,000 geometric mean covariance differences. Statistical significance is gauged by the position of the actual data statistic within the fractiles of the resampled distribution. Fig. 8 plots the bootstrapped sampling distribution? for this illustrated example, (precrisis to crisis geometric mean covariance difference for Asia). The point estimate (3.63) lies completely outside the sampling distribution and is thus statistically significant.

A similar but distinct method is used to develop a resampling distribution for testing across regions. For example, we might like to know whether Asia and Europe had statistically different covariances within the crisis period. The point estimate is \( \gamma\_{cov\_Asia,Crisis} - \gamma\_{cov\_Europe\_Crisis} \). In this case, a pair of countries is selected at random from the sixteen available and their covariance is computed from the 391 crisis period observations. The pairwise selection is repeated (with replacement) to obtain 56 resampled covariances, a number ordained by the fact that each region of eight countries has 8(7)/2 = 28 distinct **true** covariances. The 56 resampled covariances are then divided randomly into two groups, the geometric mean is computed within each group and their difference, \( \gamma\_{cov\_Group#2,Crisis} \) is taken. Repeating this operation 10,000 times provides the sampling distribution required.

For inter-regional comparison of efficient frontier curvature for a given period, a slight modification is required. If the same country were selected twice in a bootstrap pseudo-region, the covariance matrix would be singular by construction, thus implying infinite curvature. Consequently, eight different countries must be selected at random. Efficient frontier curvature is computed

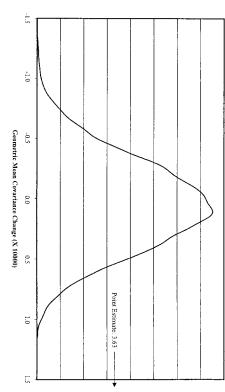


Fig. 8. Non-parametric estimated density for change in covariance from pre-crisis to crisis period, Asia.

using the covariance matrix of those eight and compared with the corresponding curvature for the eight countries not selected. The difference in the two curvatures, tabulated 10,000 times, provides the bootstrap resampled distribution.

Table 4 reports all the results. The two left columns provide evidence on the differences between the crisis and pre-crisis periods for each region considered separately. The two right columns give comparisons between the Asian and European regions by sub-period.

There are strong indications that covariances, correlations, and volatilities increased during the crisis in both regions.<sup>8</sup> All the *p*-values are 0.0000, thus firmly rejecting the hypotheses that these parameters remained constant over time. Prior to the crisis, covariances were not significantly different in Europe and Asia but they became significantly higher in Asia during the crisis. Correlations were significantly higher in Europe in both periods. Volatility was significantly higher in Asia in both periods though the magnitude of the difference and its level of significance increased during the crisis.

The  $\eta$  statistic, which measures the relative contribution of correlation to the change in covariance between periods, (see (5)), is 0.309 and 0.359 for Asia and

<sup>&</sup>lt;sup>7</sup>The bootstrapped data are fit with a non-parametric density estimator using the Gaussian kernel and a bandwidth determined by the normal reference rule. See Scott (1992, Chapter 6).

<sup>&</sup>lt;sup>8</sup>A recent paper by Forbes and Rigobon (1999) suggests that observed increases in correlations should be interpreted with caution. They argue that "... when stock market volatility increases, standard estimates of cross-market correlations will be biased upward". In the appendix to this paper, we present a counter-argument, which concludes that no such bias is actually present in our sample.

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Comparisons across periods and regions of diversification potential

Geometric averages of covariances, correlations, and volatilities are calculated from USS-denominated daily index returns for eight Asian and eight European countries before and during the 1997 Asian crisis. Efficient frontier curvatures are calculated for the countries within each region. The n statistic measures the relative importance of correlation to an observed change in covariance. The pre-crisis period was December 31, 1993 through July 1, 1997. The crisis period was July 2, 1997 through December 31, 1998. Changes in the statistics across the two periods and differences in the statistics across regions within each period are tabulated and compared against resampled (bootstrapped) probability distributions. The p-values (in parentheses) indicate the fractile of the bootstrapped distribution corresponding to the observed point estimate. The first column presents results for tests comparing the pre-crisis data and the crisis data while the second column presents those comparing Asia with Europe for the entire sample period.

Crisis-pre-crisis		Asia-Europe	
Covariancea			
Asia	3.63	Pre-crisis	-0.0648
	(0.0000)		(0.7869)
Europe	1.08	Crisis	2.48
	(0.0000)		(0.0055)
Correlation			
Asia	0.206	Pre-crisis	-0.251
	(0.0000)		(0.9928)
Europe	0.298	Crisis	-0.343
	(0.0000)		(0.9952)
Standard deviation (%)day)	(A		
Asia	2.069%	Pre-crisis	0.387%
	(0.0000)		(0.0030)
Europe	0.553%	Crisis	1.903%
	(0.0000)		(0.0016)
Efficient frontier curvature			
Asia	160.00	Pre-crisis	-65.1
	(0.0309)		(0.6710)
Europe	5.27	Crisis	89.5
	(0.1744)		(0.0093)
η statistic			
Asia	0.309		
	(0.8422)		
Europe	0.359		
	(0.6053)		

<sup>&</sup>lt;sup>a</sup>Convariances have been scaled upward by a multiple of 10<sup>4</sup>

Europe, respectively.  $\eta$  would be 1.0 if correlation were entirely responsible for the observed change in covariance from the pre-crisis to the crisis period while  $\eta$  would be zero if volatility were entirely responsible; hence, it appears that volatility was somewhat more responsible than correlation. However, the

p-values are insignificant for both regions. This suggests that both correlation and volatility played a role, neither being dominant in a statistically reliable sense

Efficient frontier curvature increased significantly in Asia (*p*-value 0.0309) during the crisis, which confirms that diversification opportunities declined substantially. In Europe, the efficient frontier's curvature also increased during the crisis period but only moderately and with an insignificant *p*-value of 0.1744. As measured by curvature, diversification was actually better in Asia than in Europe before the crisis, though the difference was not statistically significant. Diversification's drastic fall in Asia during the crisis reversed the inter-regional difference, which then became significant (*p*-value 0.0093).

The impressive decline in diversification potential in Asia at the time of the crisis is consistent with rational investors driving down asset values. Of course there is no way to ascertain whether a reduction in diversification actually caused the crisis or even whether it was an effect rather than a cause. Nonetheless, it appears to be an interesting smoking gun.

## 5.3. Decomposing the crisis; currencies vs. local returns 11

To this point, our perspective has been that of an international portfolio manager who focuses on returns in a home currency. This explains why we translated individual country returns into a common currency, the U.S. dollar. Another perspective might be that of an international economist or of a central banker who would naturally wonder about the role played by exchange rates in a crisis, as distinguished from the role played by local currency-denominated real equity returns.

Real returns cannot be easily computed on a daily basis because most countries report inflation only for monthly or even longer intervals. We can, however, examine nominal local returns. This should provide a fairly reliable picture because inflation has low volatility compared to equity returns in most countries. Rather than carry out additional formal tests, we thought it would

<sup>&</sup>lt;sup>9</sup>The reader may wonder why the Asia–Europe curvature difference of –65.1 was not significant pre-crisis while the +89.5 crisis difference was highly significant even though it is not all that much larger in absolute value. This seeming puzzle is explained by differences between the bootstrapped resampling distributions. The pre-crisis period had more than twice as many observations (913 vs. 392) and the efficient frontier curvature's sample volatility increases with sample size. Intuitively this phenomenon must be related to higher apparent (as opposed to true) diversification potential in smaller samples; i.e., mean curvature also increases with sample size, ceteris paribus.

<sup>&</sup>lt;sup>10</sup>It is, of course, conceivable that diversification potential within a region taken in isolation masks an offsetting potential of countries in the region when considered in the context of a globally diversified portfolio. However, this would only occur if the regional countries experience decreases in covariances on average with non-regional countries.

<sup>&</sup>lt;sup>11</sup>We are grateful to the referee for bringing up the issue discussed in this section.

be sufficient to simply plot our statistical constructs computed from local returns and compare them with the previous plots. Figs. 2 (bis) through 6 (bis) provide the results. Each figure is plotted on the same scale as its corresponding dollar-denominated Figs. 2–6.

Figs. 2 and 2 (bis) show, not surprisingly, that currency depreciation and currency volatility played a major role in the Asian crisis. Mean returns are much more negative when denominated in dollars (Fig. 2a) than when denominated locally (Fig. 2 (bis) a). In contrast, there is only a minor difference between the two figures for European countries. Similarly, while European volatility is virtually indistinguishable between dollar and local returns, Asian volatility is considerably higher for most countries in dollars, thus revealing that currency fluctuations represented a substantial portion of the generally higher crisis period volatility. However, the degree of this currency volatility effect differs markedly among the Asian countries. Hong Kong, for instance, has none because it maintained a fixed exchange rate with the dollar throughout. Taiwan also has roughly the same volatility in local currency as in dollars. All other countries have higher volatility in dollars. Korea, Malaysia, and Thailand have about 20–25% more volatility in dollars while Indonesia's is twice as large.

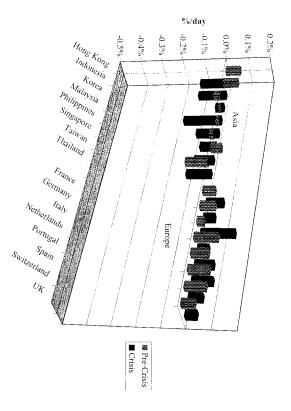


Fig. 2. Panel A (bis). Mean returns by region and period in local currencies

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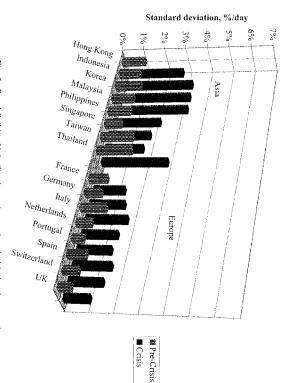


Fig. 2. Panel B (bis). Volatility by region and period in local currencies

Turning now to the contrast between dollar-denominated and local currency denominated statistics, Figs. 4 and 4 (bis) show that average correlations were very similar. They are slightly lower in dollars, but any differences in the time pattern are barely distinguishable. Thus, our previous conclusion, that (1) European correlations were higher than Asian correlations both before and during the crisis and (2) Both regions experience an increase in correlation in the crisis, is unaffected by the currency denomination.

This is definitely not true for covariances. Fig. 3 shows the geometric average covariance in Asia rising to well over  $6 (\times 10^{-4})$  during the crisis when returns are denominated in dollars, but Fig. 3 (bis) shows an increase of only half that magnitude. In contrast, the European rise in covariance is actually slightly higher near the end of the crisis if returns are locally-denominated. Clearly, currency had a dramatic effect on the covariance matrix of Asian returns. As discussed above in describing Figs. 2a and b, volatility was also influenced substantially by currency for many Asian countries, though not for European countries. This is apparent in a comparison of the geometric average volatilities in Figs. 5 and 5 (bis).

Finally, the Jennrich statistic, a measure of changes in the covariance matrix, is similar whether calculated in dollar or in local returns. Prior to the crisis, the p-value was above 10% for most periods, indicating little statistically reliable



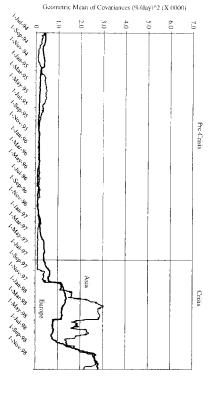


Fig. 3. (bis). Regional average covariances in local currencies.

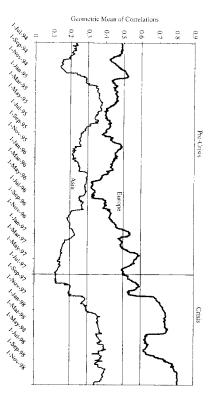


Fig. 4. (bis). Regional average correlations in local currencies.

evidence of variation in the covariance matrix. During the crisis, the *p*-values were quite small for both Europe and Asia, thereby suggesting formally that the entire covariance matrix was changing intertemporally within both regions. For Asia, the low *p*-value persists throughout the crisis period when returns are dollar-denominated. As shown in Fig. 6 (bis), however, it rises above 10% toward the end of the crisis; this suggests that intertemporal variations in the

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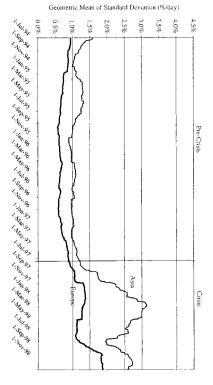


Fig. 5. (bis). Regional average volatility in local currencies.

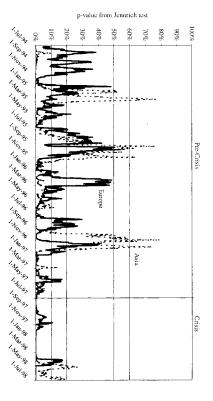


Fig. 6. (bis). Jennrich test of equality in successive covariance matrices: in local currencies.

covariance matrix became mainly attributable to currencies at that point in time.

### 6. Conclusions and future research

The 1997 Asian "crisis" brought staggering declines in equity values and exchange rates, which other regions escaped. Though painful to Asian

investors, this episode provides an opportunity for analysis and study. Perhaps we can learn something about precipitating factors in financial debacles and uncover ways to mitigate or even avoid them. Here, we offer a clinical comparison of the diseased patient, Asia, and a healthy patient represented by Europe. Our focus is on volatility spillover and diversification potential within each region. The basic idea is to examine and compare the two patients' financial fluids in an effort to understand the affliction.

To aid in this diagnostic endeavor, we design and apply some new statistical equipment to succinctly measure patterns of return co-movement and volatility within a region. These include general measures of covariance, correlation, volatility, and diversification potential.

In the three-and-a-half years prior to the crisis, Asian countries as a group had slightly higher volatility but somewhat lower correlation than their European counterparts. The general level of covariance was roughly the same in the two regions. There was no evidence of volatility spillover; i.e., return shocks were not propagated from a country to its neighbors in either region.

An increased level of return volatility and co-movement accompanied the onset of the crisis. Both Asia and Europe experience statistically significant increases in covariance, correlation, and variance. Correlation actually increased somewhat more in Europe than in Asia, <sup>12</sup> but this was swamped by much larger increases in covariance and in volatility in Asia. The volatility and covariance increases were both almost four times larger in Asia. This was exacerbated by the sudden appearance of volatility spillover, highly statistically significant in the case of Asia.

Diversification potential, as measured (inversely) by the curvature of the sample efficient frontier, tells a compelling story. Before the crisis, diversification was actually more potent within the Asian region, due perhaps to closer ties among countries within the European community than among the more diverse Asian economies. During the crisis this situation was reversed. Asian diversification potential became much worse. Its change from the pre-crisis to the crisis period was statistically significant and it fell behind Europe's diversification potential by a statistically significant margin. A large loss in diversification potency reduces the overall benefit of investing. That alone could precipitate sizable declines in asset values, though obviously we cannot know whether the observed change was a cause or an effect of the crisis.

A better understanding of regional interdependence will require something beyond stock returns. Capital movements, and event studies of major crisis incidents would be informative. A better understanding of the seeming link

between stock market movements and currency devaluations is also crucial. But no one is quite sure yet just how and why currency changes impact stock returns or vice versa. It would also be interesting to ponder theoretical reasons for the empirical findings in our clinical investigation.

The empirical procedures introduced here could be used unmodified in the study of industry linkages—to ascertain how industry or sectoral indices relate to one another and how that relation evolves over time. They could be applied with equal ease to study the relations among different stock exchanges within a country. They could measure the impact of legislation, policy changes, or technological innovations on the relations among industries within a country. Thus, we hope this clinical study will help in the diagnosis and resolution of other interesting cases.

# Appendix A. Higher correlation in more volatile times: Bias or Fact?

Forbes and Rigobon (1999) (FB) argue that increased correlation during more volatile periods could be an artifact. They derive a "bias" in the correlation coefficient and apply an adjustment for the bias to three episodes, the 1987 crash in the U.S., the 1994 Mexican peso collapse, and the 1997 Asian crisis. Since the adjustment is strictly toward zero, they derive smaller correlations in all instances and thereafter find little evidence that these crises were characterized by "contagion," i.e., by higher positive inter-market correlations.

An appendix to their paper entitled "Proof of the Bias in the Unadjusted Correlation Coefficient" contains everything necessary to understand their argument. Adopting their notation, the true structural model is assumed to be

$$y_t = \alpha + \beta X_t + \varepsilon_t,$$

where  $\beta \neq 0$  and the disturbance  $\varepsilon$  has standard spherical properties and is uncorrelated with x.

Now suppose we have two groups of observations, one with higher x volatility than the other. FB show, though it's rather obvious, that when the volatility of x increases while the volatility of x remains the same, the correlation between x and y must increase (in absolute value).

It is crucial to understand a point not mentioned by FB. The two "groups" with differing x volatility could be (a) two different regimes during which x has disparate true volatility or (b) two sets of observations sorted by observed sample volatility. A bias exists only in the latter case.

In the former case (a), an increase in the volatility of x, ceteris paribus, obviously increases the true  $R^2$  of the structural model and raises the absolute value of the correlation between x and y; (the sign of the correlation depends, of course, on  $\beta$ ). In such a circumstance, higher volatility of x would be

<sup>&</sup>lt;sup>12</sup>However, the relative increase in correlation was higher in Asia since it was considerably lower in the pre-crisis period. Within each region, volatility was slightly more responsible for the covariance increase than was correlation. (This is measured by our \(\eta\) statistic, defined in equation 5 of the text.)

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associated *correctly* with higher volatility of y and higher correlation between x and y. On the other hand, if the true volatility of  $\varepsilon$  increased while x's volatility remained unchanged, the correlation between x and y would decrease even though the volatility of y would increase.

The above structural model specialized to a group of markets can be written as

$$r_{j,i} = \alpha_j + \beta_j f_i + \xi_{j,i},$$

where the subscript j indexes the country, r is a return, and f is some underlying driving factor. (Since countries are usually positively correlated, the  $\beta_j$ 's are positive). Clearly, the general level of volatility (in the r's) could increase during a crisis because f's volatility increases or because the volatilities of the  $\xi_j$ 's increase, or both. Correlation among the r's would increase if the root cause were f but it would decrease if the cause were  $\xi$ . This implies that there is no necessary connection between a general increase in volatility during a crisis and an increase in correlation. The fact that both volatilities and correlations seem to have increased during many crises is merely consistent with a rise in f volatility relative to  $\xi$  volatility.

FB seem to have in mind case (b) where both f and  $\xi$  have constant true volatilities but data miners have picked out a sub-sample of abnormally volatile f's. Since the true correlation is constant in this scenario, the correlation coefficient estimated from the sub-sample really is biased away from zero.

The basic issue, then, is whether crises have been identified because volatility just happened to be larger than usual. The crises studied by FB were characterized most obviously by dramatic declines in asset values. But a negative average return is a phenomenon related to the mean of the distribution, not necessarily to the variance. The increase in volatility after the onset of these crises was a fact discovered later, after they had already become infamous episodes. We do not, therefore, think any adjustment is necessary and, indeed, that such an adjustment would inappropriately bias estimated correlations downward from their true values.

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